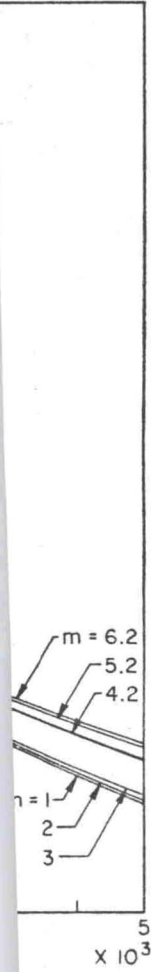


$$\begin{aligned}
 & - am)^2 + 4amA \\
 & + am)^2 - 4am \\
 & P + a) + (1 + A - \\
 & - A + am) + 2mP \\
 & 0, (q)^{1/2} < (1 + A + \\
 & > (q)^{1/2} \text{ for all } P \geq 0 \\
 & B2 \text{ is appropriately wr} \\
 & \text{form} \\
 & + am) + 2mP - (q)^{1/2} \\
 & + am) + 2mP + (q)^{1/2}
 \end{aligned}$$



answer the question for  $C > 0, (K_0' - m) < 0$ . We write equation B3 for  $q$  with  $A = K_0' - m, a = -2(K_0' - m)/C$ :

$$\begin{aligned}
 & \left[ 1 - \frac{2(K_0' - m)^2}{C} - \frac{2m(K_0' - m)}{C} \right]^2 \\
 & \quad + \frac{8m(K_0' - m)}{C} \\
 & \left[ 1 + \frac{2K_0'(m - K_0')}{C} \right]^2 \\
 & \quad - \frac{8m(m - K_0')}{C} \tag{B5}
 \end{aligned}$$

We note that both the second term and the square root of the first term in the above expression are positive; therefore,  $2bx + c > 0$  for all  $P \geq 0$ , and we again use the logarithmic form (Equation B4) to evaluate equation B2. After having evaluated the integral, equation B1, for both cases subject to  $V = 1$  when  $p = 0$  we then write the equation for  $V$  (equation 9).

APPENDIX C

As has been emphasized by Anderson [1966], the success of Murnaghan's equation 10 is spectacular because the entire curve of  $K/K_0$  versus  $K_0$  is determined by a single parameter  $K_0'$ . Moreover, this parameter is not adjusted to fit

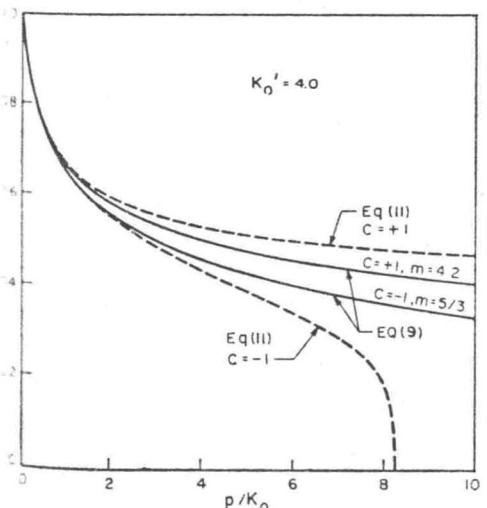


Fig. 9. Comparison of extrapolation formulas for  $C = \pm 1$  (see text).

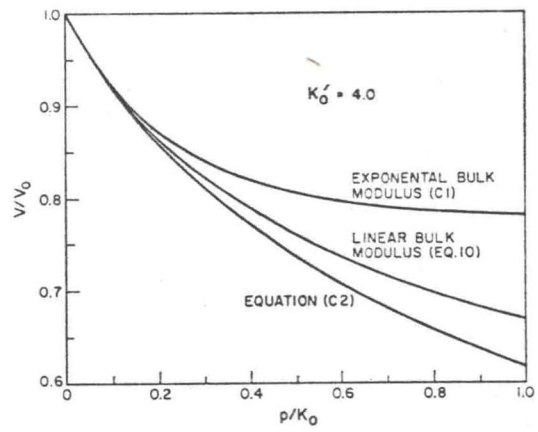


Fig. 10. Comparison of extrapolation formulas based on the linear and exponential assumptions for the bulk modulus (see text).

all the data, but only the low pressure ultrasonic data on wave transit times versus  $p$ . (This is presumed to give, after calculations using thermal data to convert from adiabatic to isothermal values of  $dK/dp$ , the true limit of  $dK/dp$  as  $p \rightarrow 0$ .) It was desired to see whether a one-parameter fit (in which the parameter is the initial value of  $dK/dp$ ) is sensitive to the assumption of exact linearity of  $K$ . To gain some insight into this question, we have compared  $V$  predicted from the linear assumption (given by equation 10) with  $V$  predicted from each of two exponential formulas.

$$\frac{K}{K_0} = \exp\left(\frac{K_0' p}{K_0}\right) \tag{C1}$$

$$\frac{K}{K_0} = \exp\left(\frac{K_0' p}{K}\right) \tag{C2}$$

With  $K$  given by equation 6 the above expressions can be integrated to obtain the required formulas for the volume ratio. From (C1),

$$V = \exp\left\{\frac{1}{K_0'} [\exp(-K_0' P) - 1]\right\} \tag{C1a}$$

and from (C2)

$$V = \exp\left\{-\frac{1}{K_0'} \left[\ln \frac{K}{K_0} + \frac{1}{2} \left(\ln \frac{K}{K_0}\right)^2\right]\right\}$$

$$P = \frac{1}{K_0'} \left(\frac{K}{K_0} \ln \frac{K}{K_0}\right) \tag{C2a}$$

The assumption (C2) leads to the above pair of equations C2a, from which calculations can